Klausur: 41050 Mathematical Methods I Wintersemester 2015/16 Prüfer: apl. Prof. Dr. F. Werner

Working time: 60 minutes

The derivation of the results must be given clearly. The statement of the result only is not sufficient.

Tools:

- pocket calculator (according to the instructions of FWW)

- either one individually prepared one-sided A4 sheet of paper with arbitrary material (write '1' on cover sheet) or textbook 'Mathematics of Economics and Business (write 'B' on cover sheet)

It is not allowed to use mobile phones.

Problems:

- 1. (a) An arithmetic sequence has the first term $a_1 = \frac{20}{3}$, the constant difference $d = \frac{8}{3}$ and for some *n* the partial sum $s_n = 896$. Determine the corresponding value of *n* and the term a_n .
 - (b) Check by means of the quotient criterion whether the series

$$\sum_{n=1}^{\infty} \frac{2^{n-1}}{3^n \cdot n^3}$$

converges.

(12 points)

2. (a) Given are the functions

$$f: [0,6] \to R_f$$
 with $f(x) = 4x - 1$

and

$$g: [-2,2] \to R_g$$
 with $g(x) = \sqrt{8-x^3}$.

Determine the ranges R_f and R_g of the functions f and g as well as the composite functions $f \circ g$ and $g \circ f$ provided that they exist.

(b) Determine

$$\lim_{x \to 3+0} \frac{\ln(2x-5)^2}{\sqrt{x^2-9}} \, .$$

(12 points)

3. Given is the function $f : \mathbb{R}_+ \to \mathbb{R}$ with

$$f(x) = \frac{40x}{1+x^2} \, .$$

- (a) Determine all local extreme points of function f and their type.
- (b) Determine all monotonicity intervals of function f.
- (c) Determine all $x \in D_f$ for which function f is convex.
- (d) Check whether the function f is elastic for some $x \in D_f$.

(19 points)

4. Using integration by substitution, find

$$\int \frac{\sqrt[3]{x}}{1+\sqrt[3]{x}} \, dx \, .$$

(7 points)